DOE/PC/95051--T1

Measurement Techniques For Local and Global Fluid Dynamic Quantities in Two and Three Phase Systems

RECEIVED

DEC 1 1 1996

OSTI

TOPICAL REPORT

FINAL DRAFT

DOE Contract DOE-FC 22-95 PC 95051

S. Kumar, M. P. Duduković

Chemical Reaction Engineering Laboratory
Washington University
St. Louis, MO - 63130

and

B. A. Toseland

Air Products and Chemicals, Inc. PO Box 25780 Lehigh Valley, PA 18007

March, 1996

Cleaned by Podew Counsel US/DOE PATENT CLEARANCE IS REQUIRED PRIOR TO THE PUBLICATION OF THIS DOCUMENT.

MASTER

DISTRIBUTION OF THIS DOCUMENT IS UNLIMITED

ELEARED BY PATENT COUNSEL

DISCLAIMER

Portions of this document may be illegible in electronic image products. Images are produced from the best available original document.

Disclaimer

This report was prerepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor army agency thereof, nor any of their employees, makes any warranty, i, express or implied, or assumes any legal liability or responsibility for r the accuracy, completeness, or usefulness of any information, apparatuse product, or process disclosed, or represents that its use would note infringe privately owed rights. Reference herein to any specific commmercial product, process, or service by trade name, trademark, manufacturer, or otherwise does not necessarily constitute or imply its endorsemment, recommendation, or favoring by the United States Government o or any agency thereof. The views and opinions of authors expressed h herein do not necessarily state or reflect those of the United States Government or any agency thereof.

DISCLAIMER

Portions of this document may be illegible electronic inmage products. Images are produced frrom the best available original document.

Contents

A	ostra	ıct	111
E	cecut	tive Summary	iv
1	Intr	roduction	1
2	Gas	Holdup and Solidds Concentration Measurement	1
	2.1	Global Techniques	2
	2.2	Line Average Measumrements based on Radiation Techniques	6
	2.3	Probes for Local Gasas Holdup and Solids Concentration Measurement	16
		2.3.1 Impedance PProbes	16
		2.3.2 Optical Probbes	19
		2.3.3 Other Probess	20
3	Mea	asurement of Bubbble Sizes and Velocity	22
4	Mea	asurement of Liquidid and Solid Velocities	29
5	Fin	al Recommendationns and Remarks	37
6	Nor	menclature	39
7	Ref	erences	41

Abstract

Available measurement technniques for evaluation of global and local phase holdups, instantaneous and average phase velocities and for the determination of bubble sizes in gas-liquid and gas-liquid-solid systems are r reviewed. Advantages and disadvantages of various techniques are discussed. Particular empphasis is placed on identifying methods that can be employed on large scale, thick wall, high ppressure and high temperature reactors used in the manufacture of fuels and chemicals from synthesis gas and its derivatives.

Executive Summaryy

This report presents a criticalal review of the methods available for assessing the fluid dynamic parameters in large industrialal two and three phase bubble column and slurry bubble column reactors operated at high pressure and temperature. The physical principles behind various methods are explained, and thhe basic design of the instrumentation needed to implement each measurement principle is discussed. Fluid dynamic properties of interest are: gas, liquid and solids holdup and their axial a and radial distribution as well as the velocity distribution of the two (bubble column) or three e phases (slurry bubble column). This information on operating pilot plant and plant reactors is essential to verify the computational fluid dynamic codes as well as scale-up rules used in 1 reactor design. Without such information extensive and costly scale-up to large reactors that exploit syngas chemistries, and other reactors in production of fuels and chemicals, cannot be avoided. The fluid dynamic parameters mentioned above must be measured under operating conditions in large units and the data used for evaluating existing models.

The findings of this studyly can be summarized as follows. While many promising techniques based on conductancee, impedance, ultrasound, light transmittance and other principles are emerging, none has yet reached the status of being capable of providing reliable measurements in high temperature, high pressure, large diameter columns operated in the churn turbulent regime with high gas and solids holdup. Hence, further development of these techniques in the laboratory ε should be encouraged.

The following methods seeem most suitable at the moment for providing the fluid dynamic parameters in industrial columns such as the Laporte AFDU reactor.

For global gas holdup meæasurements, determination of the dynamic height of the slurry in an operating reactor (by a a gamma ray or other means) and of the settled slurry in the absence of gas provides the bleast ambigous value of overall gas holdup. During shut down the dynamic gas disengagement technique is capable of providing global information on the existence of unimodal or muliltimodal bubble size distribution. Overall solids holdup can be determined from the volume e of the solids loaded and the height (volume) of the slurry at operating conditions.

Best estimates of gas hololdup during operation, and its distribution along the column height, can be obtained via a sectional pressure drop measurements. This estimate requires the knowledge of the solids occoncentration distribution which is not always available.

Density profiles along the e column can be obtained by gamma ray densitometry (a needed correction for obtaining propeer cross sectional values from the usually measured chordal averages is discussed in this report). Cross-sectional density distribution can be readily obtained

by gamma ray tomography. Obtaining gas holdup profiles along the column height, or in a cross section, again requires i information (or assumptions) regarding solids concentration distribution. Solids concentration profiles can be obtained noninvasively by dual beam gamma ray tomography using sourcees with photon emissions at two different energy levels. This may require excessive scanning titimes. Invasive isokinetic sampling or point conductance probes represent the unappealing althernative in hot and high pressure systems for the measurement of local velocity and/or phases concentration. Ultrasound probes deserve further attention and can be suitably designed to provide local measurements of phase concentrations.

While sophisticated technniques such as Particle Image Velocimetry (PIV) and Computer Aided Radioactive Particle Tracking (CARPT) can be used in the laboratory to map the velocity fields, at present the eir use in industrial reactors is not possible. To determine liquid velocities, pitot tubes seem t to be still favored, while gas (bubble) velocities can be assessed by multipoint optical probess. How well these can work in systems with high solids loading remains to be demonstrated. Only CARPT is capable of determining solids velocities at high solids holdup, and this,; unfortunately, cannot be implemented for large reactors.

Specific recommendations for the Laporte reactor can be summarized as follows:

- 1. Continue to use gamma densitometry and implement gamma ray tomography for noninvasively obtaining desensity distributions along and across the column at all operating conditions.
- 2. Develop if possible dua al beam densitometry by adding the Am-241 or Co-60 source to the current Cs-137 source. This would enable one to resolve the gas, liquid and solids holdup profiles in the c column at all operating conditions.
- 3. Install additional presssure taps for the measurement of sectional pressure drop along the column, and also monitor pressure fluctuations and compute cross-correlations between various points.s.
- 4. Prior to each shut down execute the dynamic gas disengagement method and evaluate the bubble size distribution.
- 5. Consider installing invasive probes for the estimation of phase velocities. Pitot tube, five point optical probees and heat transfer probes are the current likely candidates.

1 Introduction

Design and scale-up of bubbble columns, slurry bubble columns, three phase fluidized beds and other multiphase systemms are still predominantly based on empirical correlations validated over a limited range and operating conditions and physical properties. Application of more fundamental fluid ddynamic models awaits their experimental verification. Hence, measurement of fluid dynamic quantities such as phase velocities, phase holdups, bubble size etc. are of great interest botth for extending the range of validity of current correlations and for verification of fundamental hydrodynamic models. Measurement is also important in interpreting, understanding and predicting reactor performance. Advances in instrumentation and signal processing techniques have led to a rapid proliferation of the available experimental methods for measurements in multiphase flows. There are a number of good reviews of these methods in the literature including those by Banerjee and Lahey (1981), Delhaye (1986), Jones and Delhaye (1976), Snoek (1990) and Lubbert, (1991) to mention a few.

An attempt is made heree to present a comprehensive review of the experimental methods available for multiphase e systems. The emphasis is on techniques that can be utilized under conditions of interest i in practice such as high pressure and temperature, large solids holdup etc. The measurement methods for the determination of the following quantities are considered:

- Void fraction and solidds concentration;
- Bubble size distribution and rise velocities;
- Liquid and solid phase e velocities.

2 Gas Holdup and Solids Concentration Measurement

Gas holdup and solids concenntration measurement methods can be broadly classified into two categories: (1) those providing an overall or global measurement and (2) those that provide a local or point measurement. The global measuring techniques yield information on the line, area or volume averaged gass or solids holdup. The volume averaged or overall fractional holdup of a phase is defined I as the fraction of the volume of the multiphase dispersion that is occupied by that phase. I In general, the measurement of the overall holdup is relatively simple. It provides informatation regarding what fraction of the system volume is occupied by the phase of interest. Measurement of the phase fraction at a point is in itself not of much use unless the distribution of such point measurements is obtained in space. If such

point measurements are obtained using some kind of invasive probe (as is done most often), then obtaining the distribution of the local phase volume fraction involves a tedious data collection process. This, in adddition to their intrusive nature constitutes a serious drawback in using probes to obtain the e local phase holdup in two or three phase flow systems.

2.1 Global Techniques

The simplest method of measuring the overall fractional gas holdup in two phase systems is rather straight forward. The \dot{z} knowledge of the volume occupied by the phase of interest as well as the volume of the expanded multiphase dispersion suffices for the needed calculation. For a system with uniform croross-section the process involves the measurement of the height of the dispersion H_g at operatiting conditions and that of the static column (with no gas flow), H_0 , and calculating the gas hholdup from :

$$\epsilon = \left(H_g - H_0\right) / H_g \tag{1}$$

Frequently an accurate meeasurement of the height of the dispersion is not possible either due to the fluctuation of the lelevel of the free surface due to bubble disengagement (especially at high gas flow rates) or due e to the formation of foam at the free surface of the dispersion. Generally, an average of severeral observed readings is adopted to minimize the error in the measurement. Although, mosst often the height of the dispersion is obtained directly, with the aid of a length scale, otherer methods have also been used. A novel method involving the use of a hot film anemometer: has been used by Deckwer et. al. (1980) for determination of the free surface of the dispersision in a slurry bubble column. The hot wire was first calibrated in the gas and the slurry phaase. With the top of the column as reference, the hot wire is moved down towards the susppension and, when it touches the slurry phase, the heat removal and, hence, the electric currennt, increases sharply thereby enabling an accurate measurement of the local height of the disppersion. Clark (1987) has used a neutron based technique for detecting the free surface of i the slurry in a high pressure bubble column. The method is based on the ability of the liquid phase to scatter more neutrons than the gas. The gas liquid interface is detected by moviring the assembly of the neutron source and detector down the reactor until a decrease in the neutron flux is detected. The precision of interface detection is reported to be ± 5 mm. These method can also be implemented using a γ ray source instead of the neutron beam. All thhese methods, however, still contain an error associated with the fluctuation of the free suurface. In addition, the measurement made of the free surface is local and instantaneous. (Consequently, a true average can be obtained by making the measurement at different points and at different instants of time.

For non-transparent columns, as in most industrial situations, the position of a float can be used for detecting the freee surface. The position of the float, as it moves with the free surface of the dispersion, is t transmitted either through a system of linkages or a string and pulley arrangement to a pointner moving along a length scale. This method has the advantage in that the float dampens out some of the fluctuations of the free surface of the dispersion.

Another method that has been adopted for obtaining the overall fractional phase holdup in two phase systems is to ininfer it from the measurements of the pressure drop along the height of the column. The tltheoretical background for the technique has been presented by Hills (1976), as well as by Melerchuk and Stein (1981). In gas-liquid systems, if the liquid flow rate is small then, to a goodd approximation, the pressure drop can be wholly attributed to the hydrostatic head as:

$$\frac{dP}{dh} = -\rho_l g (1 - \epsilon) \tag{2}$$

where h is the axial coordinate pointing upwards and ρ_l is the liquid (two phase system) or slurry (three phase system) density. The actual measurement can either be of the static pressure, or of the differential pressure using manometers or some kind of a pressure transducer. If dz represents the height ϵ difference observed in a differential manometer, the following expression holds:

$$\rho_l g \frac{dh}{dz} = \frac{dP}{dz} + \rho_l g \tag{3}$$

From these expressions it follows that

$$\epsilon = \frac{dz}{dh}$$

If, however, the liquid flow rate is not negligible, one has to account for the wall shear stress and for the effects of a acceleration of the liquid due to voidage changes. Eq 2 must be augmented to include terms the for these, and the resulting expression for the void fraction is

$$\epsilon := \frac{dz}{dh} + \frac{U_l^2}{g} \frac{d}{dz} \left(\frac{1}{1 - \epsilon} \right) + \frac{4\tau_w}{\rho_l D_c g}$$
 (4)

where U_l is the liquid superfricial velocity, τ_w is the wall shear stress and D_c is the column diameter. Eq. 4 constitutes a an implicit expression for the overall void fraction. In addition its solution requires some method of determining the wall shear stress for a given flow condition. Generally this is done in terrms of the friction factor, f. For single phase flows f is obtained from the charts as a function of the Reynolds number. The same approach has been adopted

by Hills with the assumption 1 of a pseudohomogeneous two phase mixture for the dispersion. Merchuk and Stein (1981) uses the correlation of Nassos and Bankoff (1967) for the friction factor expressed in terms of tithe Reynolds number defined for two phase flow.

Fig. 1 illustrates the prinnciple of the differential pressure gradient method. In general, when this technique is adopted the terms corresponding to the friction and the acceleration effects are usually neglected. The lower the gas flow rate, the better this approximation is. One can also use this methodd to obtain an averaged void fraction in sections of the column by the measurements taken I by a series of pressure taps situated along the column height (Prakash and Briens, 1990, RReilly et. al., 1986, Merchuk, 1986, Nicol and Davidson, 1988). The phase fraction obtained it is an average over the volume of the dispersion located between

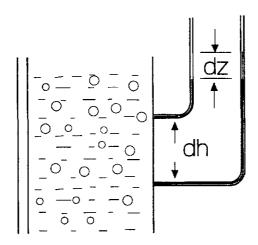


Figure 1: Principle for r holdup measurements by means of differential pressure.

the corresponding pressure taaps. The method is fairly simple to work with and is applicable to systems at high temperatuures and pressures. When one of the phases is a solid, the other being a gas or liquid, then it i is necessary to take precautions against clogging of the taps by means of filters or by flushing the taps by a low flow rate of gas. In three phase systems one must also know the solids conncentration as a function of height unless the slurry behaves as a pseudohomogeneous mixturire.

The overall void fraction c can also be measured by what is referred to as the quick closing valves technique (Rosehart etet. al., 1975, Colombo et. al., 1967, Yamaguchi and Yamazaki, 1982). It is based on isolatizing the two phase dispersion between two sections of the test loop and then measuring there mass of the continuous phase. This, along with the known geometrical parameters and I the pressure in the system, can be used for estimating the

holdup between the two sectctions. The necessary simultaneous closure of two valves that isolate a section of the system is achieved either by coupling the two valves mechanically by springs or by making use of scolenoid valves. Although this can be a very accurate method of obtaining a volume averaged d gas holdup, it is mainly applicable to small diameter columns. In larger installations the values may have considerable time constants for closing. Also this method is mainly employed f for gas-liquid systems. It can be also be used for gas-solid and liquid-solid systems with mooderate solids loading.

Impedance void meters are based on the principle of measuring the electrical impedance of the two phase dispersion. (Gas (air) and liquid (water) have significantly different electrical conductivity and permittivity, and this technique exploits this difference. The variation in the flow structure is accompanied by a variation in the impedance of the two phase mixture which is measured by metallicic electrodes introduced suitably in the flow. The void fraction is then estimated by adopting a a relative impedance technique. The system can be implemented so that the impedance is governed by the conductance or the capacitance or both. It has to be noted that the impedance of the mixture that is sensed by the electrodes depends not only on the void fraction but also on its distribution (flow regime). The void fraction is calculated as a function o of the dielectric constants of the two media using theoretical relations. A relation that has sound wide acceptance for low void fractions is the one derived by Maxwell (1881) shown here

$$\frac{\kappa_m - \kappa_w}{\kappa_m + 2\,\kappa_w} = \epsilon \, \frac{\kappa_v - \kappa_w}{\kappa_v + \kappa_w} \tag{5}$$

where κ is the dielectric consistant, with subscripts m, w and v signifying the mixture, water and vapor, respectively. Another relation for the slug flow regime is

$$\epsilon = \frac{1 - c/c_0}{1 - \kappa_v/\kappa_w} \tag{6}$$

where c and c_0 represent the c capacitance of the mixture and the liquid, respectively. As noted by Cimorelli and Evangelisticic (1967) the reliability of all such relations is poor and direct calibration for each flow regizime is necessary. The technique can be adopted to provide an average over a volume whose size can be large or small, and, accordingly, the measurement can be considered as global o or local.

For three phase systems; no single method can provide both the solids and overall gas holdup. The expansion of solids (when larger solid particles are used) due to the fluidization by either liquid or gas can be measured in a manner similar to the bed expansion method discussed earlier. Three phases fluidized bed reactors are generally of the continuous flow

type and hence the initial beæd height corresponds to the height of the reactor up to which the solids are filled. The bed I is then fluidized by either only the liquid phase or a premixed gas-liquid stream. The operatiting conditions are generally such that the solids are not carried along by the fluids but rather ϵ expand to a certain elevation within the column. Once a steady state of operation is established, there exist two distinct regions in the flow referred to as the three phase region and the freeboard region. The height of the three phase region is measured as the expanded beed height. The overall solids holdup in the three phase region is calculated using the expression:

 ϵ_s = Vol. of solids loaded / Vol. of three phase dispersion

If measurements from anotherer technique, such as the pressure drop method are available, the individual gas and liquid holddups can also be obtained in conjunction with the solids holdup obtained from the bed expansision. Since, solids holdup in such systems is often a function of the vertical position in the eccolumn, this technique only provides the overall gas and liquid holdup in the three phase reggion. In gas-sparged slurries with small solid particles, the liquid-solid slurry is most often approximated as a pseudohomogeneous liquid. An effective density is obtained, and the nmethods described for gas-liquid systems can then be used.

Recommendation: For estimation of the overall fractional gas holdup one should measure the pressure profile along the reactor length and provide a rough comparison for it by the bed expansion method. The height of the dispersion in the slurry column can be obtained by a γ -ray densitonmeter (such as the one already in use at Laporte). Table 1 provides a comparison of the e characteristics of the available methods for overall gas holdup measurement.

2.2 Line Average M/leasurements based on Radiation Techniques

A holdup measurement that c can be considered to be in between the overall and point measurement is based on absorptition of radiation. Extensive reviews of this technique have been written by Hewitt (1978), Joones and Delhaye (1976), Banerjee and Lahey (1981), and by Snoek (1988). A good introduction of the principles behind some of the techniques has been presented by Schrock (1969).

In most applications it is 3 the attenuation of the radiation (X-rays or gamma-rays) that serves as the basis for the mmeasurement. The absorption of a narrow beam of radiation of initial intensity I_o by a homogeneous material with a mass attenuation coefficient μ is expressed as:

Table 1: Utility of Different Techniques for Overall Gas Holdup Measurement

	Bed Expansion	Pressure	Quick Closing	Impedance Void
	Method	Gradient Method	Valves	Meters
Intrusiveness	1	1	2	3
Applicability in Applicability in Aqueous Systems	Yes	Yes 1 es	Yes	No (Capacitive two (Capacitive meters)
Applicability in Hydrocarbon Systems	Yes	Yes	Yes	No (Conductance meters)
Applicability in 3-Phase systems	Yes	Not sufficient [®]	Yes	No
Accuracy	3-4	2-3	1-2*	2
Ease of Use & Adaptability	1	2	ಸು	ణ
Cost of System	1-2	2-3	4	ဇာ

Numbers in table indicate a ranking on a scale of 1 to 5. Rank 1 indicates that the technique is most suitable and rank 5 signifies that the technique is not to be preferred. Ranking for the cost of the system is based on 1 representing the least expensive and 5 representing the most expensive system.

^{*} provided valves close rapidly and simultaneously

[®] an additional measurement by an independent technique is required

$$I = I_0 \exp(-\rho \mu l) \tag{7}$$

where I is the intensity of radiliation detected after the beam has traveled a distance l through the absorbing medium. For i a mixture of two substances, say a gas and a liquid with an attenuation coefficient μ_g and μ_l and densities ρ_g and ρ_l , respectively, the corresponding relation is

$$I = I_o \exp[-(\rho_g \mu_g l_g + \rho_l \mu_l l_l)]$$
 (8)

where l_g and l_l are the path l lengths of the beam in the gas and the liquid, respectively. In terms of the measured intensisities I_{tp} , I_f and I_{mt} corresponding to the test section with the two-phase mixture, full of liquid and completely empty, respectively, the chordal average void fraction is computed from:

$$\epsilon = \frac{\ln(I_{tp}/I_f)}{\ln(I_{mt}/I_f)} \tag{9}$$

This expression is applicaable only in two-phase systems and only when a narrow collimated beam is used in the mmeasurement process. However, many early studies have used what is referred to as the onne shot method wherein an uncollimated beam of radiation as wide as the test section of intiterest is used. Use of Eq. 9 in conjunction with this method is known to result in large errors because of the dependence of the attenuation process on the distribution of the voids i.e., ς on the flow regimes.

In principle, the void fraaction profile can be determined to a fine detail by having a source emitting a narrow bearam of radiation and an opposing detector scan across the cross-section. This yields a series ϵ of chordal average measurements. To obtain a distribution of the void fraction across a giveren cross-section, one would have to obtain a series of such scans at different angular orientatitions. The process of obtaining the voidage profile from such measurement is commonly referered to as tomography. Figure 2 illustrates the differences in the data collection procedureses of densitometry and tomography.

For industrial systems it i is convenient and less expensive to obtain a few chordal measurements of the attenuation through the test section. Unfortunately, it is often forgotten that a single line averaged holodup, even if it is obtained across the centerline of the column is not representative of the coross sectional mean. The line averaged holdups along several chordal positions can, however, be used to obtain a cross-sectional mean provided that one assumes that the holdup distitribution is axisymmetric. If such an assumption can be made, the radial variation of the holdup and hence the cross-sectional mean can be obtained by

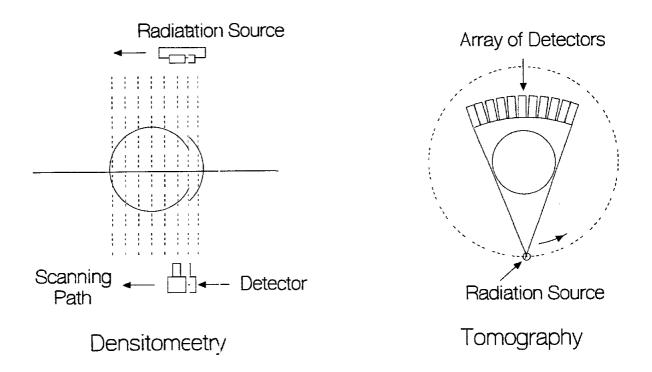


Figure 2: Datata collection for densitometry and tomography.

making use of the Abel integgral and its inversion.

If f(r,R) is a function of i radial position that is nonzero only within a circle of radius R, then its Abel transform is

$$\phi(x,R) = 2 \int_0^{\sqrt{f(R^2 - x^2)}} f\left(\sqrt{(x^2 + y^2)}, R\right) dy = 2 \int_x^R \frac{f(r,R) r}{\sqrt{r^2 - x^2}} dr$$
 (10)

The above is merely the line e integral along the ray in the y direction at the position x in the x-y coordinate system. The z inversion expressing f in terms of ϕ is

$$f(r,R) = -\frac{1}{\pi} \int_{r}^{R} \frac{d\phi/dx}{\sqrt{x^{2} - r^{2}}} dx$$
 (11)

For our case, the quantitity $\varphi(x,R)$ corresponds to the quantity $\ln(I_{\circ}/I)$ divided by the corresponding chordal lengthh. Many different numerical approaches have been suggested for the implementation of the Abel inversion (Bockasten, 1961, W. L. Barr, 1962, Dong and Kearney, 1991). To illustrate that the centerline averaged holdup is an overestimate of the cross-sectional mean, and that the Abel inversion provides a radial distribution that leads to

the correct cross-sectional metean, the following simulation has been made. An axisymmetric distribution of the holdup is assumed in an air-water bubble column of 19.05 cm in diameter. The assumed radial distribution has the functional form (Kumar, 1994)

$$\epsilon(\xi) = \bar{\epsilon} \frac{m+2}{m} (1 - c \, \xi^m) \tag{12}$$

where $\bar{\epsilon}$ is the cross-sectional mean holdup, m is the power law exponent and c is a constant that provides for non-zero holdup at the wall of the column. These parameters were obtained from the experimentally determined void fraction distributions using the CT scanner at CREL (Kumar et al.]., 1995) a schematic of which is shown in Fig.3. The value

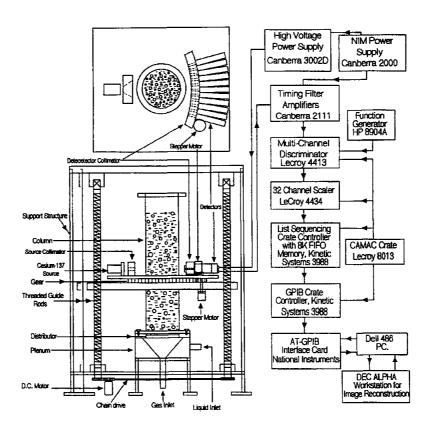


Figure 33: Schematic of the CT scanner at CREL

of the power law exponent is high for a flat holdup distribution (corresponding to bubbly flow) and decreases for the more parabolic profile that is observed in churn turbulent regime. For a given holdup distribution the line integrals corresponding to the quantity $\int (\mu_{\text{air}} \epsilon + \mu_{\text{water}} (1 - \epsilon)) \epsilon dl$ are computed. The limits of integration depend on the position of the chord. The negative exponential of this quantity would correspond to the ratio

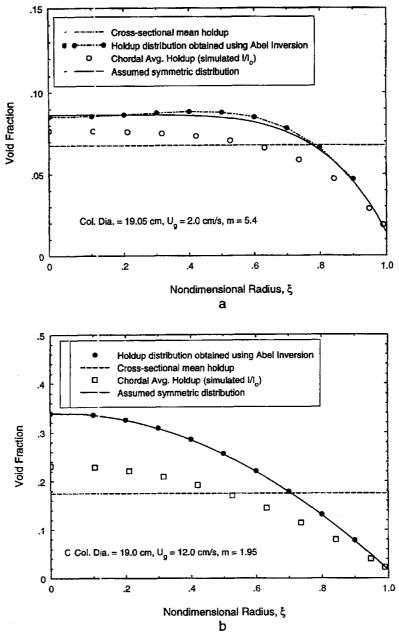


Figure 4: Comparison of f assumed distribution, chordal averages and Abel inversion

 I/I_0 that is measured in deensitemetry (as well as CT). Shown in Figures 4 (a) and (b) are the assumed symmetric holddup distributions (similar to experimentally determined holdup profiles in the two flow regimmes), and the chordal average holdups that are obtained from the simulated line integrals folor two values of m corresponding to bubbly and churn turbulent regimes, respectively. Also slshown as a horizontal line for comparison is the cross-sectional mean. The chordal average centerline holdup is always higher than the cross-sectional mean. Using the entire set c of chordal measurements, the Abel inversion provides a radial distribution that is the same c (within numerical error) as the assumed (original) axisymmetric distribution. Abel inversion c yields reliable results only when the distribution is axisymmetric. For industrial systems c the current measurement practice can be modified to provide