

## Nomenclature

$A_{\alpha\beta}, \tilde{A}_{\alpha\beta}$	matrices for determining $c_\alpha$
$B_\alpha, \tilde{B}_\alpha$	vectors for determining $c_\alpha$
$a_m, b_n$	polynomial coefficients for Abel transform
$B$	MCA energy bin number
$B_p$	MCA energy bin number of peak
$B_w$	MCA energy bin width of peak
$C_\alpha$	conductivity parameters
$c_\alpha$	increments in conductivity parameters
$c_{mn}, d_{nm}$	reconstruction coefficient matrices for Abel transform
$D$	cylinder or vessel diameter
$d_b$	diameter of a sphere with the same volume as a prescribed bubble
$f(r, R)$	inverse Abel transform of $g(x, R)$
$g(x, R)$	Abel transform of $f(r, R)$
$H_0$	height of gas-liquid interface in bubble column without gas flow
$H$	height of gas-liquid interface in bubble column with gas flow
$I$	intensity (counts per second) of gamma beam
$i, j$	FEM nodal indices
$I_e$	current scale for electrodes in EIT
$I_0$	intensity (counts per second) of gamma beam initially
$I_h$	MCA intensity height of peak
$J_n$	normal current flux
$\mathbf{J}$	current flux vector
$k, m, n, p$	FEM nodal indices for nodes at electrodes
$k_0, k_1, k_2$	parameters for Gaussian fit to peak in MCA spectrum
$L$	either path length or height of measurement above vessel bottom
$M_{ij}$	global stiffness matrix
$M_{\alpha ij}$	derivative of the global stiffness matrix $M_{ij}$ with respect to $C_\alpha$
$m_\beta, n_\beta$	conductivity function internal parameters
$N_e$	number of electrodes in EIT system
$N_n$	number of nodes in FEM representation of EIT
$N_\sigma$	number of conductivity parameters in EIT
$\mathbf{n}$	outward normal unit vector
$\Delta P$	pressure difference between two pressure transducers for DP technique
$P$	pressure
$P_\beta$	conductivity function internal parameters
$R$	cylinder or vessel radius, or domain length scale in EIT
$R_\beta$	conductivity function internal parameters
$r$	cylindrical coordinate
$s$	arc length
$s^{(k)}$	arc length location of electrode $k$ in EIT
$T$	temperature

$t$	time
$U_G$	gas superficial velocity in bubble column
$U_1$	velocity in formula for terminal bubble velocity
$U_2$	velocity in formula for terminal bubble velocity
$U_T$	terminal velocity of an isolated gas bubble in a liquid
$V$	voltage
$V^{(k)}(\mathbf{x})$	voltage field for current injection and withdrawal at electrode $k$ and node 0
$V^{(mn)}(\mathbf{x})$	voltage field for current injection and withdrawal at electrodes $m$ and $n$
$V_i^{(k)}$	voltage at node $i$ for current injection and withdrawal at electrode $k$ and node 0
$V_i^{(mn)}$	voltage at node $i$ for current injection and withdrawal at electrodes $m$ and $n$
$V_k^{(mn)}$	voltage at electrode $k$ for current injection and withdrawal at electrodes $m$ and $n$
$V_{k,1}^{(mn)}$	voltage $V_k^{(mn)}$ when $\sigma = \sigma_1(\mathbf{x};\{C_\alpha\})/C_1$ , $\alpha = 2, \dots, N_\sigma$ , and $C_1 = 1$
$V_0^{(mn)}$	arbitrary voltage offset, an adjustable parameter in EIT
$\partial V_i^{(k)}/\partial C_\alpha$	Jacobian
$v_k^{(mn)}$	experimental voltage at electrode $k$ for injection, withdrawal at electrodes $m, n$
$W$	vertical separation of two pressure transducers for DP technique
$\mathbf{x}$	coordinate vector
$x$	Cartesian coordinate, horizontal, normal to paths
$y$	Cartesian coordinate, normal to $x$ and $z$ , parallel to paths
$z$	Cartesian or cylindrical coordinate, vertical, along cylinder axis
$\alpha, \beta$	indices for conductivity parameters
$\delta_{ij}$	Kronecker delta function
$\delta(s)$	Dirac delta function
$\varepsilon$	phase volume fraction or "holdup"
$\Gamma$	rms difference between computational and experimental EIT voltages
$\phi_i(\mathbf{x})$	FEM basis function
$\psi(x, R)$	$g(x, R)/[2\sqrt{R^2 - x^2}]$
$\eta$	viscosity (absolute)
$\mu$	attenuation coefficient
$\rho$	density
$\sigma$	electrical conductivity
$\sigma_0$	representative value of electrical conductivity
$\sigma_1$	electrical conductivity function $\sigma = \sigma_1(\mathbf{x};\{C_\alpha\})/C_1$ , $\alpha = 2, \dots, N_\sigma$
$\tau$	gamma detection time constant
$\zeta$	surface tension
$(\ )_a$	pertaining to air
$(\ )_G$	pertaining to gas
$(\ )_L$	pertaining to liquid
$(\ )_S$	pertaining to solid
$(\ )_s$	pertaining to glass spheres
$(\ )_w$	pertaining to water

$[ \ ]_{av}$	average over measurement plane
BBC	boxed bubble column
BEI	bulk electrical impedance
BEM	boundary-element method, a numerical method
CMRR	common mode rejection ratio for an amplifier
DP	differential pressure
EBP	electrical bubble probe
EIT	electrical-impedance tomography
EITA3D	FEMEIT-like code for three-dimensional voltage fields, axisymmetric conductivity
FEM	finite-element method
FEMEIT	finite-element method electrical-impedance tomography code
FIDAP	commercial finite-element method code (Fluid Dynamics International)
GDT	gamma-densitometry tomography
ICI	insulating cylindrical inclusion
LR	level rise
LSF	liquid-solid flow
MCA	multi-channel analyzer
MUX	multiplexer
PSD	phase-sensitive demodulator
RTR	real-time radiography
SBCR	slurry bubble column reactor
SCA	single-channel analyzer
TBC	transparent bubble column
XRT	x-ray tomography
VCCS	voltage-controlled current source
WCD	wax/catalyst disk
2DynaEIT	boundary-element method electrical-impedance tomography code (Dynaflow, Inc.)
2DynaEIT_fwd	code to generate validation for 2DynaEIT (Dynaflow, Inc.)
ansoln	code to generate analytical voltage fields from infinitesimal strip electrodes
fuldat	code to take adjacent-electrode EIT data and generate a full EIT data set
msheit	code to generate a triangular mesh on a circular domain for FEMEIT
postfd	code to create a FIDAP neutral file for postprocessing from FEMEIT output